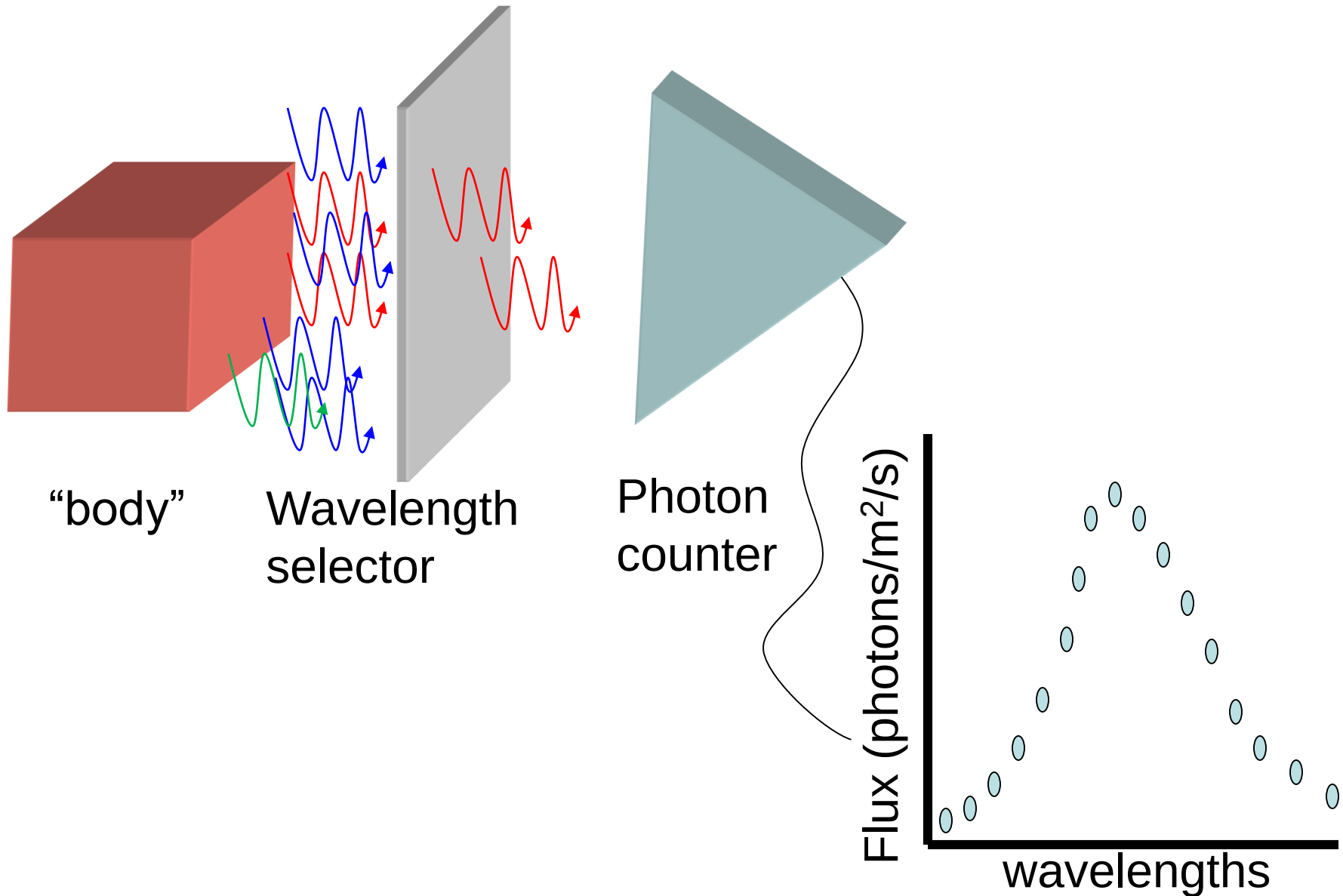
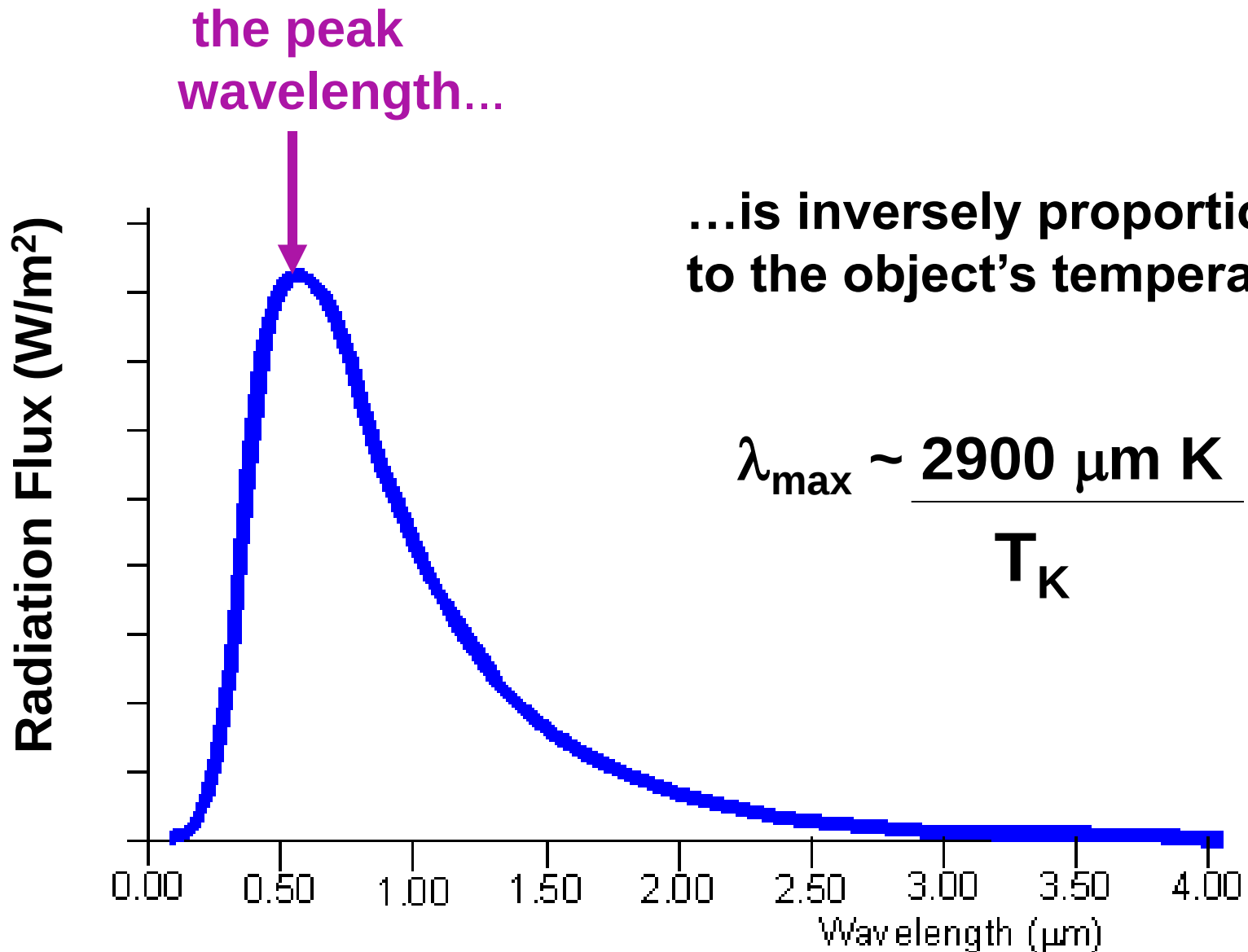


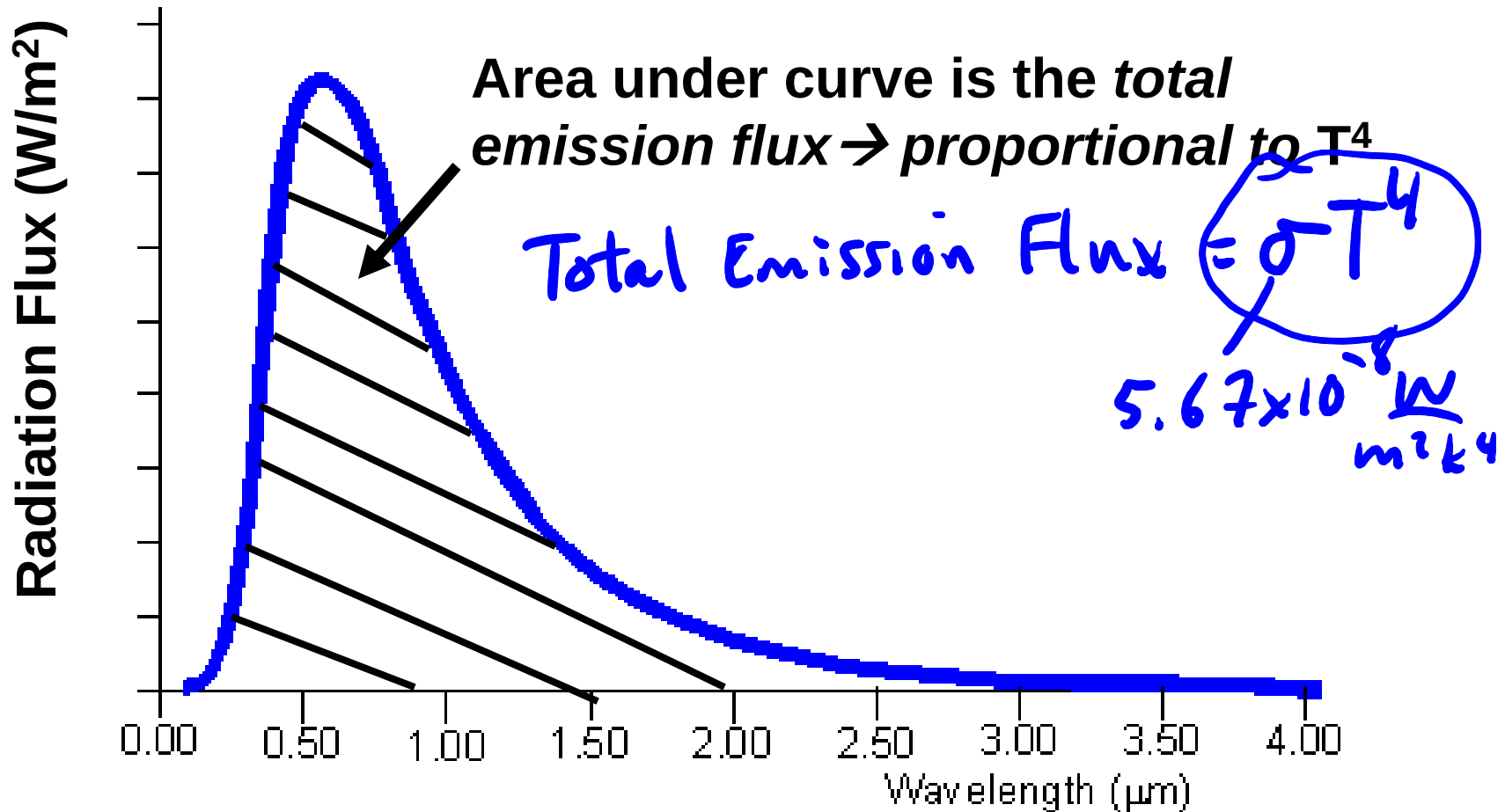
Emission Spectrum: energy distribution



Blackbody Radiation: Wien's Law



Blackbody Radiation: Stefan-Boltzmann's Law



W

The global average temperature of Earth's surface is $\sim 15^\circ\text{C}$. What wavelength carries the most radiant energy emitted by Earth's surface?

Visual settings 

Activate 

Show results 

Show correct 

Lock 

 When poll is active, respond at Pollev.com/thornton211

 Text **THORNTON211** to **22333** once to join

Clear results 

Fullscreen 

0.1 micrometer

1 micrometer

10 micrometer

Next 

Previous 

Total Results: 0

W The sun's emission flux maximizes at a wavelength of ~ 0.5 micrometer. The sun's surface temperature is

 When poll is active, respond at PollEv.com/thornton211
 Text **THORNTON211** to **22333** once to join

~ 1500 K

 ~ 6000 K

$\sim 15,000$ K

Visual settings 

Activate 

Show results 

Show correct 

Lock 

Clear results 

Fullscreen 

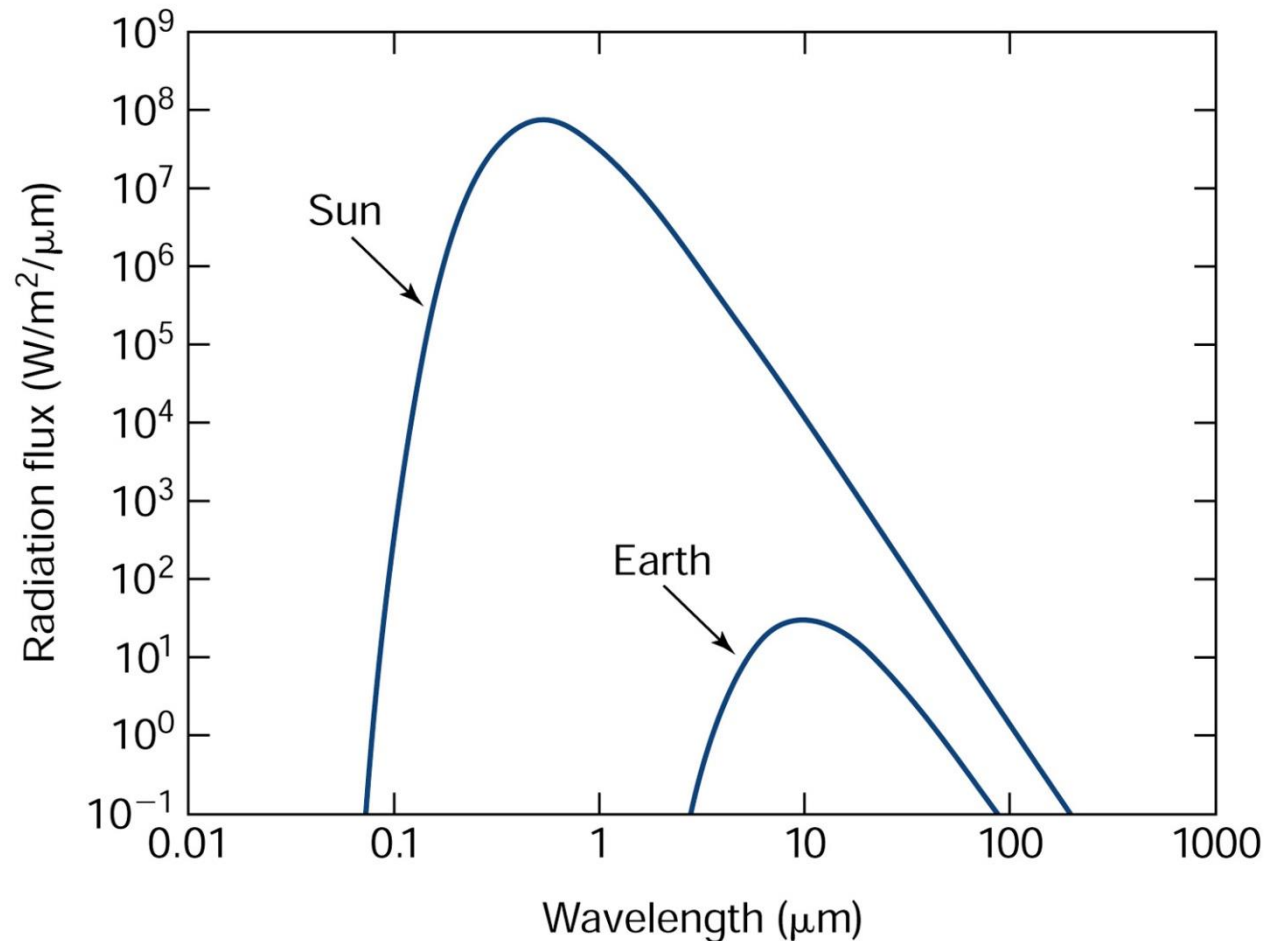
Next 

Previous 

Total Results: 0

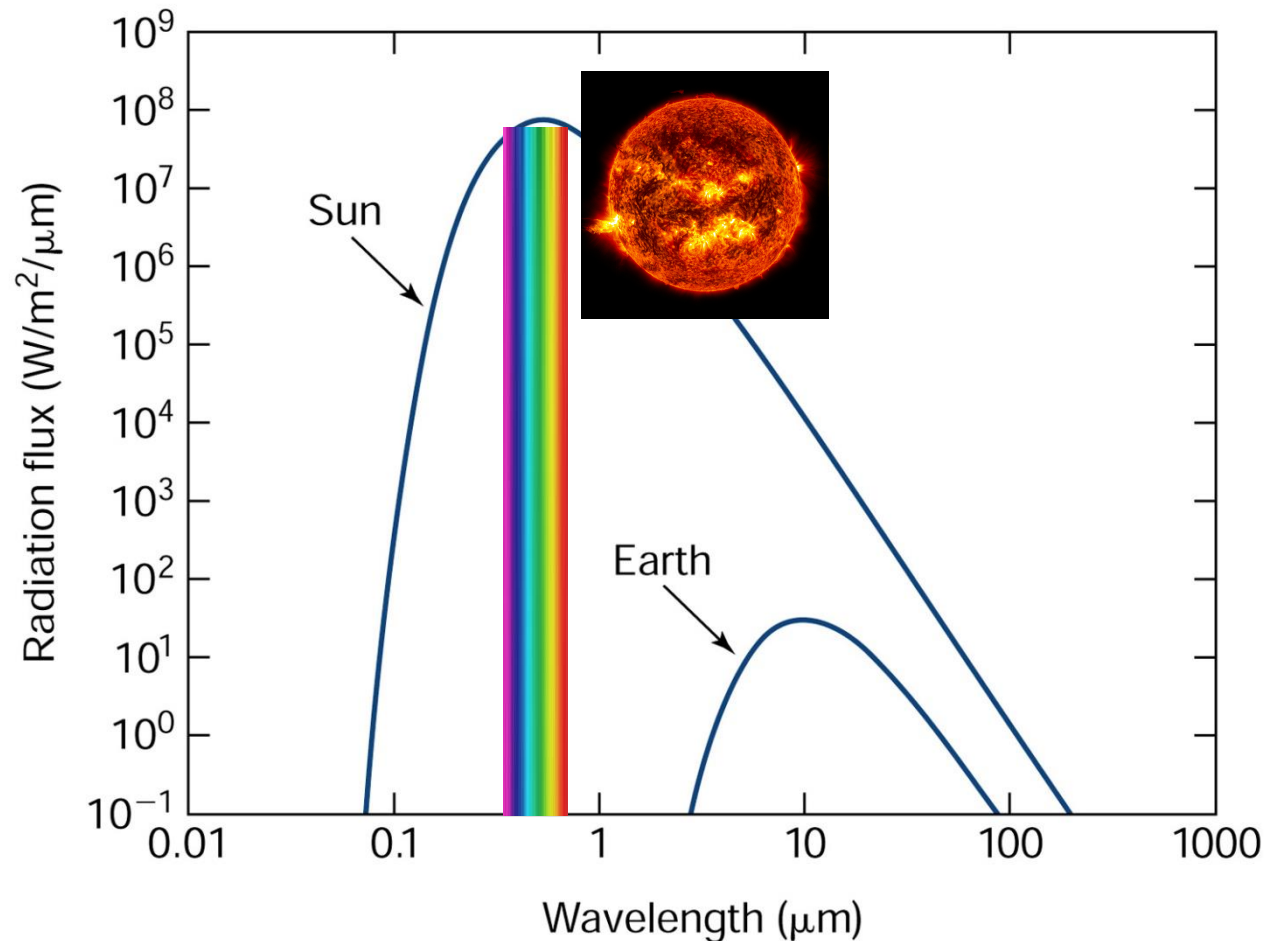
Earth and Solar Emission Spectra

The sun emits about $6.3 \times 10^7 \text{ W/m}^2$ of radiant energy

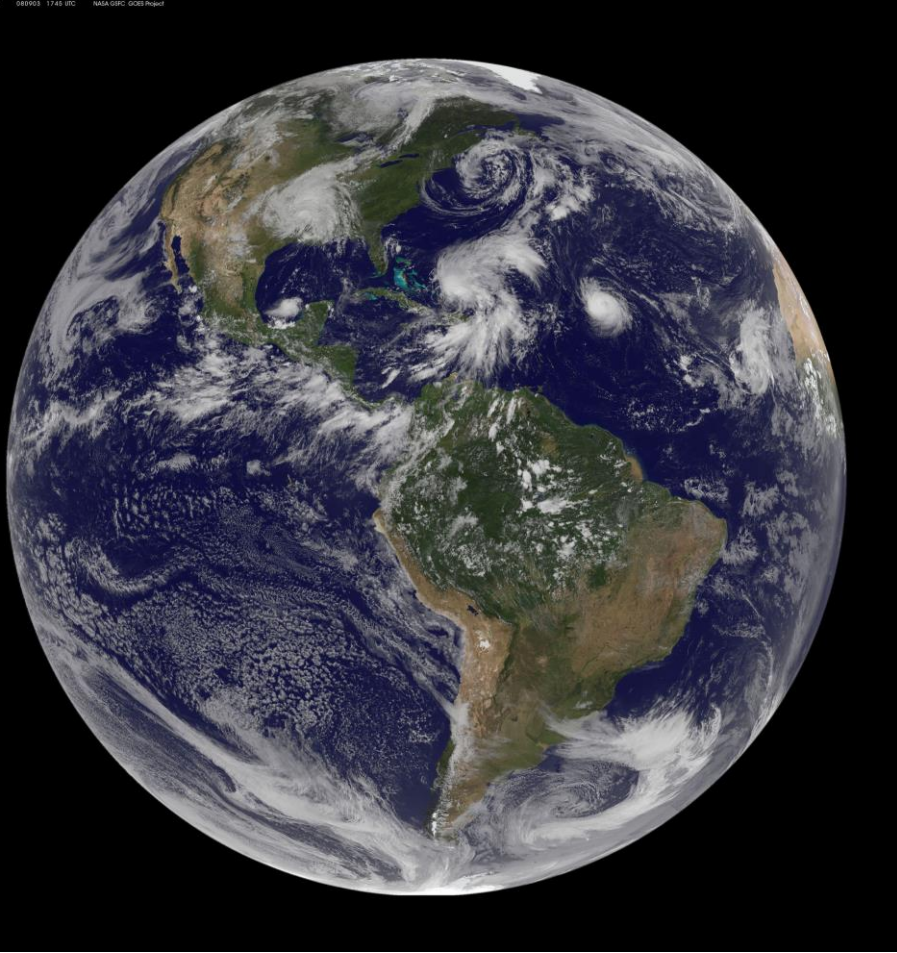


Earth and Solar Emission Spectra

The sun emits about $6.3 \times 10^7 \text{ W/m}^2$ of radiant energy



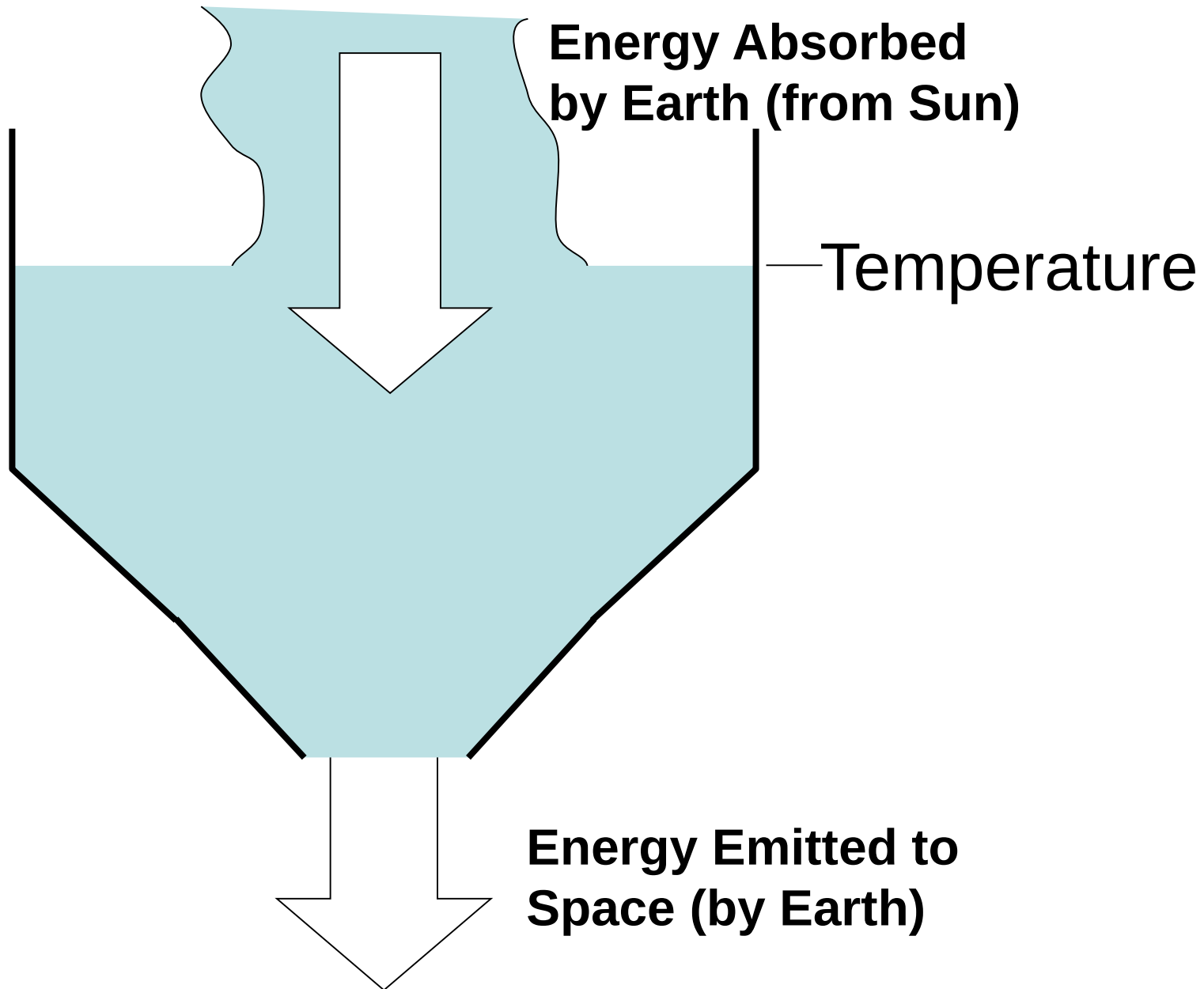
Putting Blackbody Radiation Laws to Work



A first attempt at a global climate model

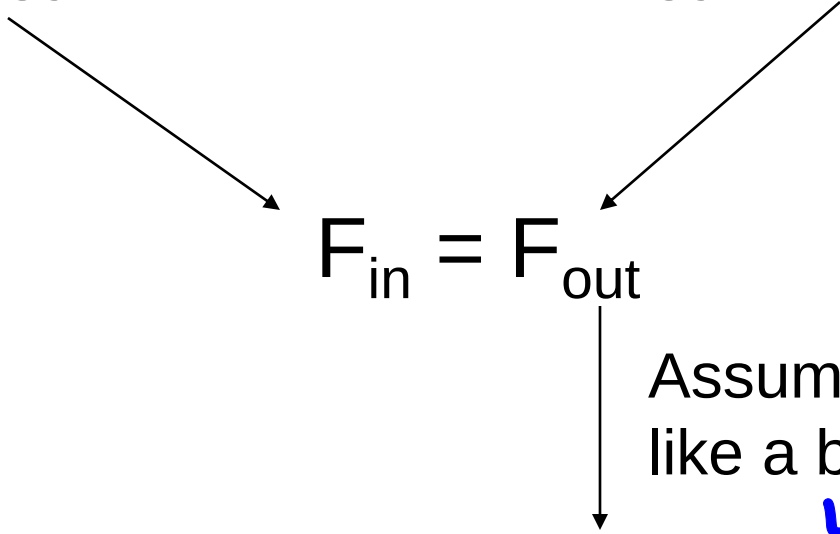
→ Relate Earth's T to incoming and outgoing radiation

An Energy Balance Model of Earth's T



Energy Balance Model: Halfway Done

Energy Flux In = Energy Flux Out



The diagram illustrates the derivation of the blackbody radiation equation for Earth's energy balance. It starts with the general principle 'Energy Flux In = Energy Flux Out' at the top. Two arrows point from this principle to the equation $F_{\text{in}} = F_{\text{out}}$ in the middle. From this equation, a vertical arrow points down to the final equation $F_{\text{in}} = F_{\text{out}} = \sigma T_{\text{Earth}}^4$. To the right of this final equation, the text 'Assume Earth radiates like a blackbody' is written, with a blue arrow pointing to the $\sigma T_{\text{Earth}}^4$ term. Next to this text, 'Stefan-Boltzmann Law' is written in blue cursive.

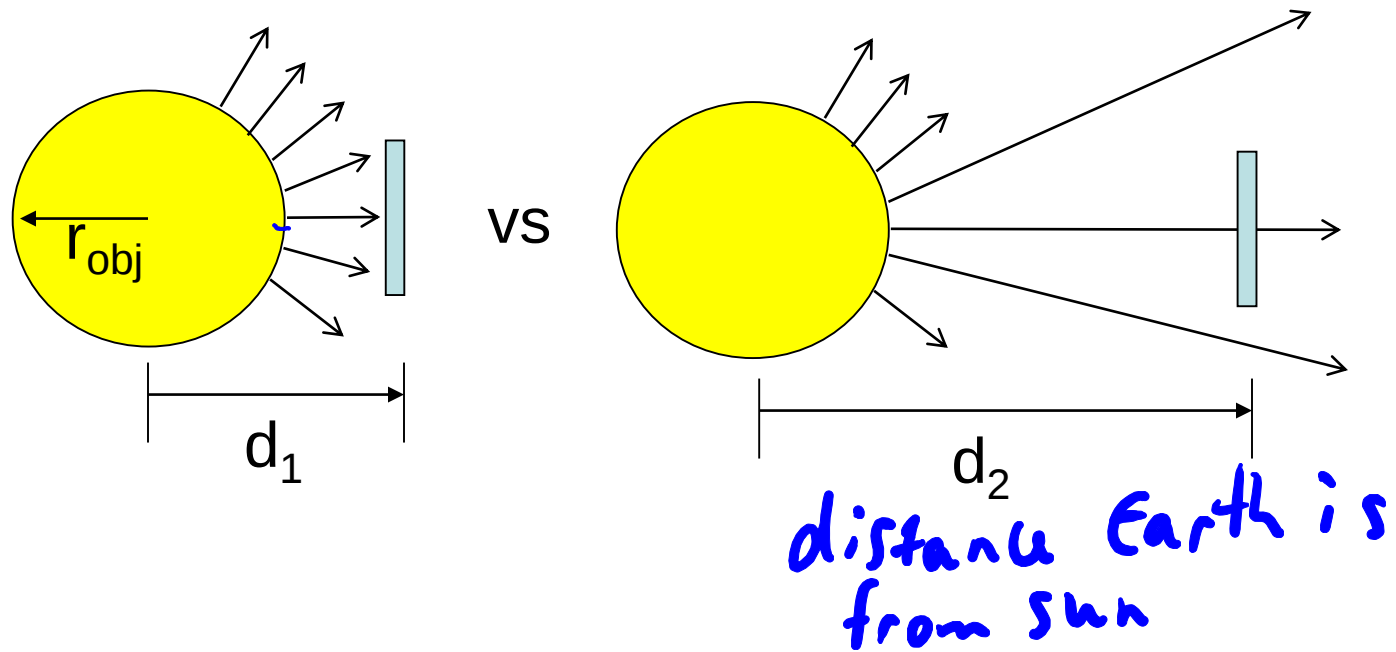
$$F_{\text{in}} = F_{\text{out}}$$

Assume Earth radiates
like a blackbody

$$F_{\text{in}} = F_{\text{out}} = \sigma T_{\text{Earth}}^4$$

Stefan-Boltzmann
Law

Radiant Energy Flux Far From Source



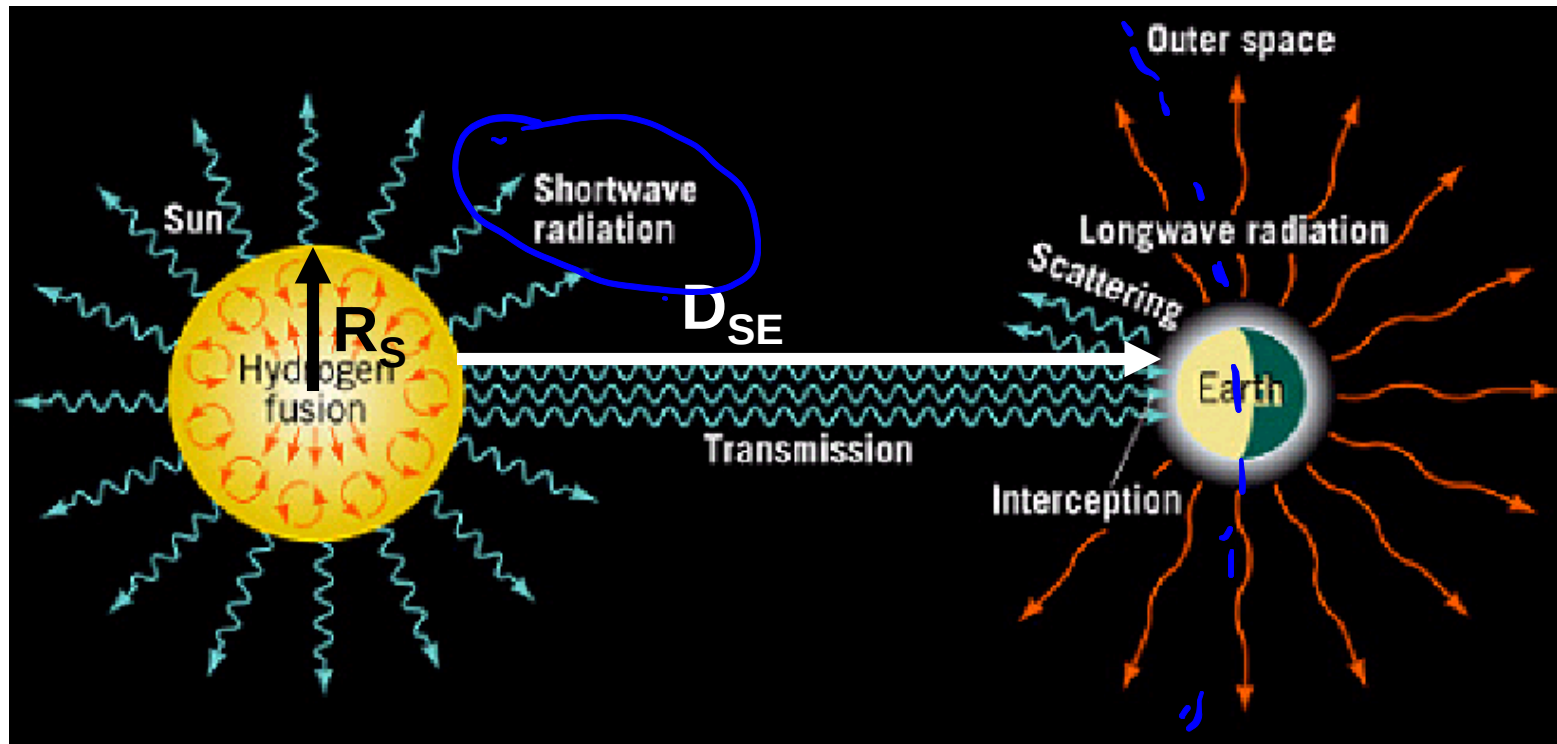
Radiation flux decreases as *inverse square* of distance from source

$$F_{d_2} = F_{d_1} * \left(\frac{d_1}{d_2} \right)^2$$

Inverse Square Law: Painting Spheres



Earth's Energy Balance: Towards F_{IN}



Need to account for

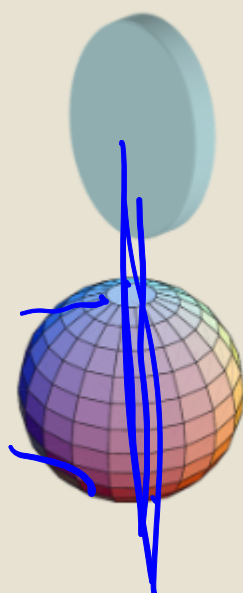
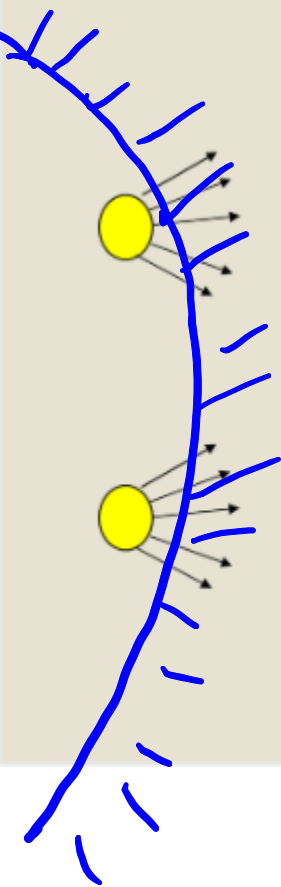
- a) Earth-Sun distance (D_{SE}),
- b) Earth intercepts fraction of total solar flux at D_{SE}
- c) Earth "reflects" some of the intercepted radiation

↳ Albedo

W

Both the disc and the sphere have the same radius. Which one will intercept the most radiation

 Poll locked. Responses not accepted.



"Area" = πr^2

"Area" = $4\pi r^2$



Total Results: 0

Visual settings 

Activate 

Show results 

Show correct 

Lock 

Clear results 

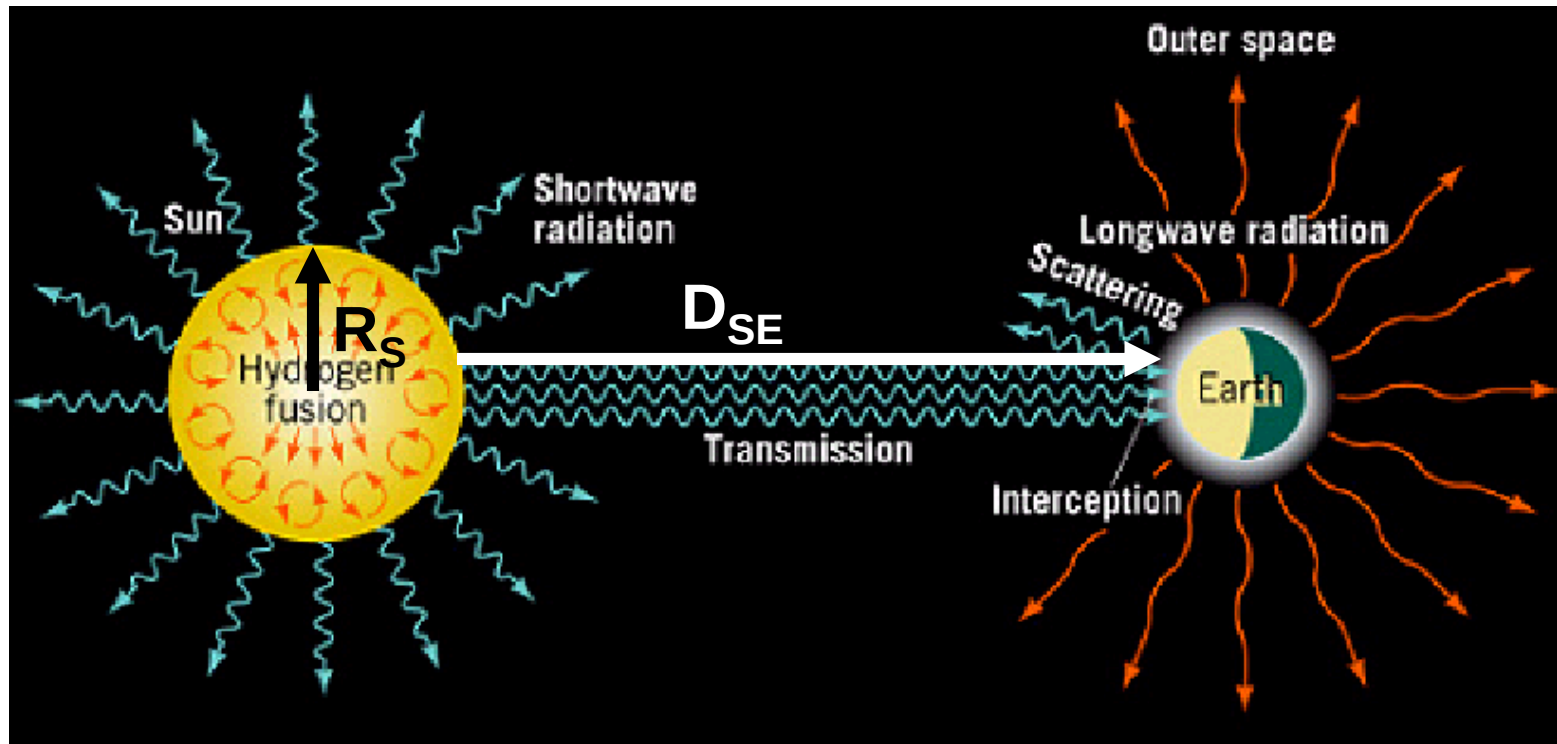
Fullscreen 

Next 

Previous 

Our own little test

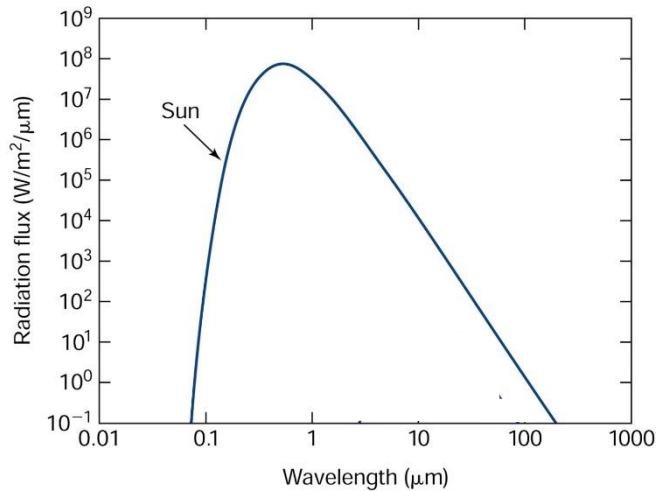
Earth's Energy Balance: Towards F_{IN}



Need to account for

- a) Earth-Sun distance (D_{SE}), ***inverse square law***
- b) Earth intercepts fraction of total solar flux at D_{SE}
- c) Earth “reflects” some solar radiation, **Albedo (“A”)**

Solar Constant (not really a constant)



Energy emitted by sun
at different wavelengths

$$F_s = \sigma T_s^4$$

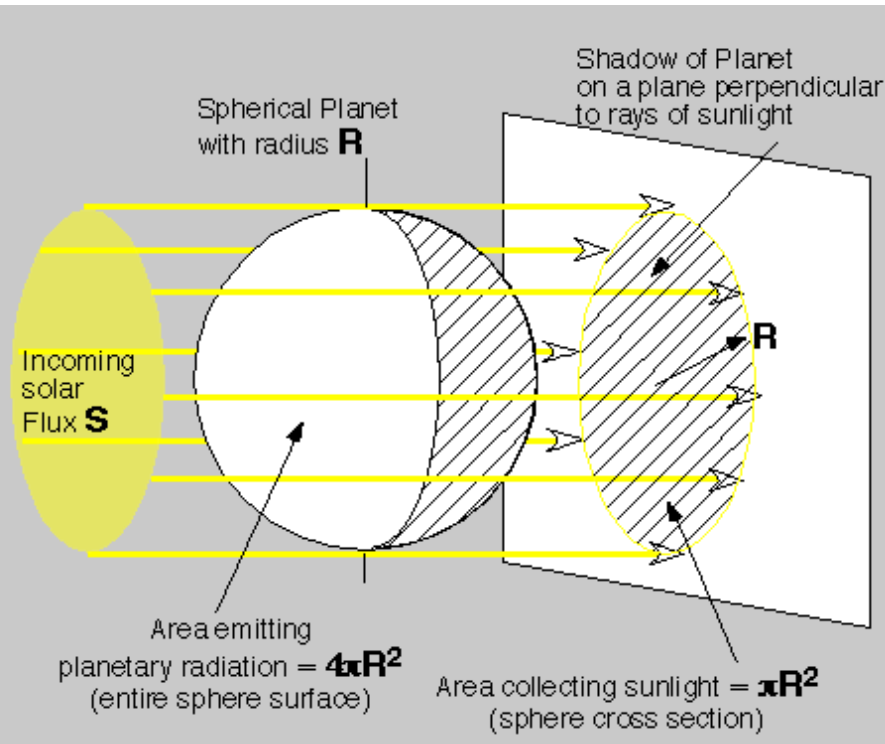
$$F_s^{OE} = \frac{\sigma T_s^4 \cdot 4\pi R_s^2}{4\pi D_{se}^2} = \text{solar constant} \Rightarrow S_0 \sim 1370 \frac{\text{W}}{\text{m}^2}$$

amount of energy reaching
location of Earth



Energy flux from sun at Earth's
location (inverse square law)

Earth's Energy Balance: Earth-Sun Geometry



Sun's energy collected by Earth

$$S_0 \pi R_E^2$$

Sun's energy collected by Earth, spread over entire Earth area

$$\frac{S_0 \pi R_E^2}{4\pi R_E^2} = \frac{S_0}{4}$$

Sun's energy collected and absorbed by Earth, spread over entire Earth area

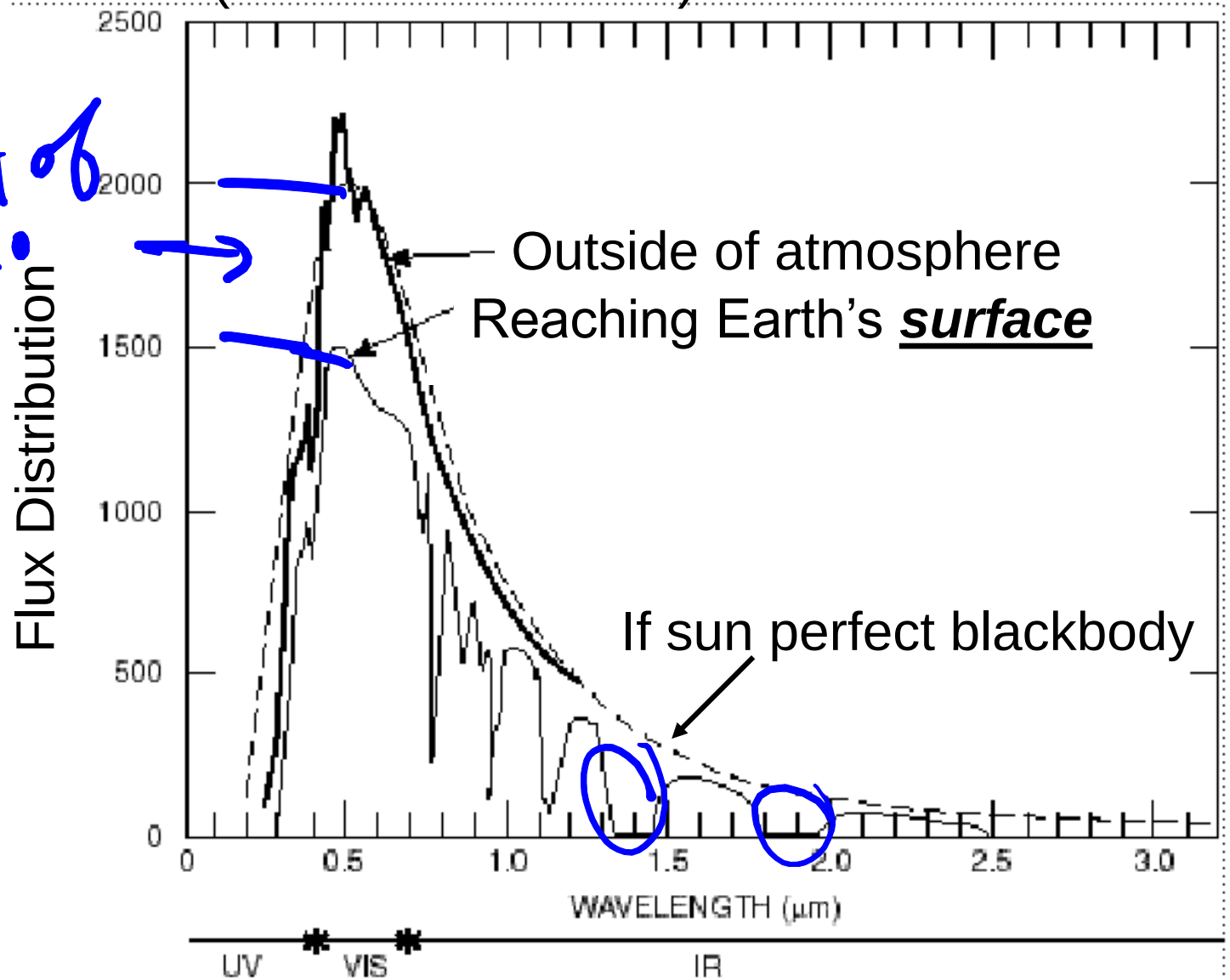
$$F_{in} = \frac{S_0}{4} (1 - \bar{A})$$

Albedo

Solar Radiation Flux at Earth

(measured at Earth)

Effect of
Albedo



Earth's Energy Balance—No Atmosphere

$$F_{\text{in}} = F_{\text{out}}$$

$$\frac{S_0(1-A)}{4} = \sigma T_E^4 \quad 0.28$$

$$T_E = \left(\frac{S_0(1-A)}{4\sigma} \right)^{\frac{1}{4}} \quad \sqrt{\quad}$$

$1370 \frac{\text{W}}{\text{m}^2}$ $5.67 \times 10^{-8} \frac{\text{W}}{\text{m}^2 \text{K}^4}$

Earth's Energy Balance—No Atmosphere

$$\begin{array}{c} \mathbf{F}_{\text{in}} = \mathbf{F}_{\text{out}} \\ \swarrow \quad \searrow \\ \frac{S_o(1-A)}{4} = \sigma T_E^4 \end{array}$$

Earth's Energy Balance—No Atmosphere

$$\begin{array}{c} \mathbf{F}_{\text{in}} = \mathbf{F}_{\text{out}} \\ \swarrow \quad \searrow \\ \frac{S_o(1-A)}{4} = \sigma T_E^4 \end{array}$$

$$T_E = \left[\frac{S_o(1-A)}{4\sigma} \right]^{\frac{1}{4}} = \underline{256\text{ K}}_{\text{Earth}}$$

Same approach for ANY planet!